## Homework Day 11 - ECON 186

Problem 1. Let $X$ be a random variable whose pmf is

$$
f(x)= \begin{cases}\frac{1}{x(x+1)} & \text { for } x=1,2,3, . . . \\ 0 & \text { otherwise }\end{cases}
$$

Find the mean of $X$.

## Problem 2.

In a class of 50 students, the number of students $n_{i}$ of each age $i$ is shown in the following table:

| Age $i$ | $n_{i}$ |
| :---: | :---: |
| 18 | 20 |
| 19 | 22 |
| 20 | 4 |
| 21 | 3 |
| 25 | 1 |

If a student is to be selected at random from the class, what is the expected value of his age?

Problem 3. Suppose $X$ is a random variable with pdf

$$
f(x)= \begin{cases}\sqrt{x} & \text { for } 0<x<1 \\ 0 & \text { otherwise }\end{cases}
$$

Find the expected value and variance of $X$.
Problem 4. Show that two random variables $X$ and $Y$ cannot possibly have the following properties:

$$
E(X)=3, E(Y)=2, E\left(X^{2}\right)=10, E\left(Y^{2}\right)=29, E(X Y)=0
$$

Hint: Find the correlation of $X$ and $Y$.

Problem 5. Compute the mean and variance of the Bernoulli distribution using the moment generating function.

Problem 6. Suppose we have two random variables $X$ and $Y$ where $E(X)=5, E(Y)=3$, $\operatorname{Var}(X)=6, \operatorname{Var}(Y)=2, \operatorname{Cov}(X, Y)=10$.
a. Compute $E(3 Y-2 X+7)$
b. Compute $\operatorname{Var}(5 X-Y+2)$

Problem 7. A random variable $X$ is normally distributed with mean 1 and variance 4. Find the value of each of the following probabilities:
a. $\operatorname{Pr}(X \leq 3)$
b. $\operatorname{Pr}(2<X<5)$
c. $\operatorname{Pr}(1 \leq-2 X+3 \leq 8)$

